



Jet Propulsion Laboratory  
California Institute of Technology

# A Citrus Census

## With Discriminative Representations for Multiple Endmember Spectral Mixture Analysis

David R. Thompson, Erika V. Podest, R. Glenn Sellar, Brian D. Bue,  
Mark Helmlinger

Jet Propulsion Laboratory California Institute of Technology

# Agenda

Introduce a new application:  
Mapping residential citrus

1

2

Describe our MESMA preprocessing:  
Multiclass LDA



# Motivation

Huanglongbing (HLB) costs hundreds of millions of dollars in damages to Florida and Texas orchards.



Early detection in California is critical to an effective response, but 50% of citrus is outside commercial groves



# Mapping concept



10/28/13

2013 HypIRI Science Workshop -  
Realtime cloud screening

# Mapping concept

Sponsored by California Citrus Research Board

AVIRIS-C flew over LA citrus hotspots (~20 flightlines)

Aim to detect and identify individual plants

Challenges:

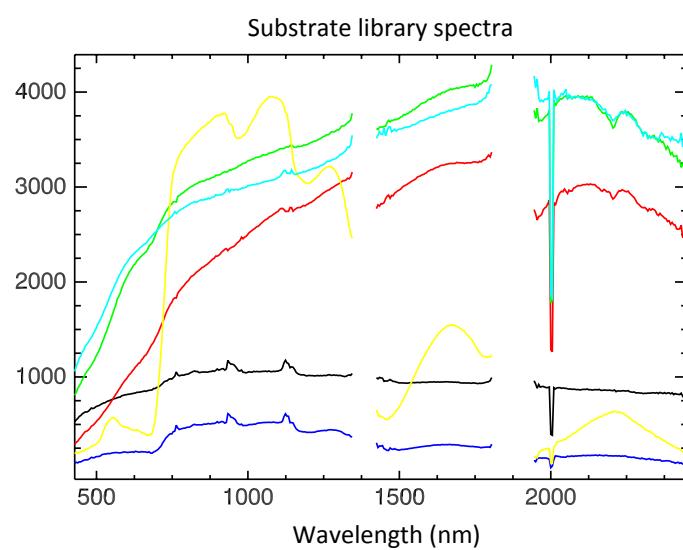
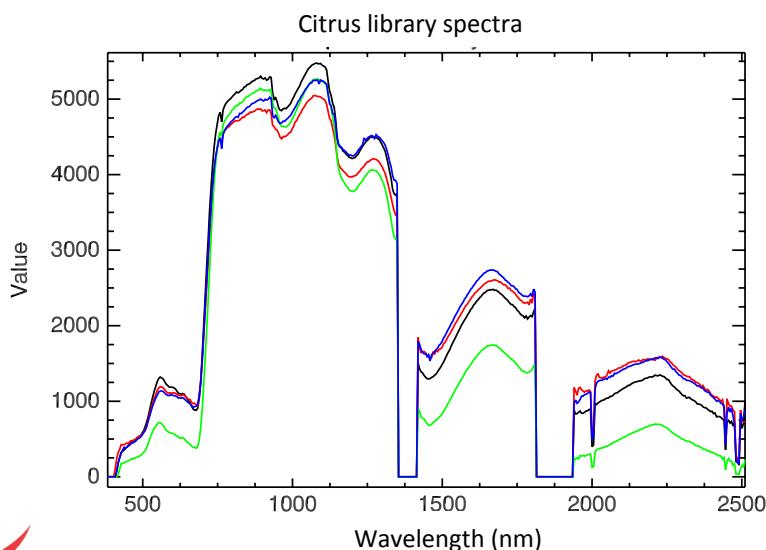
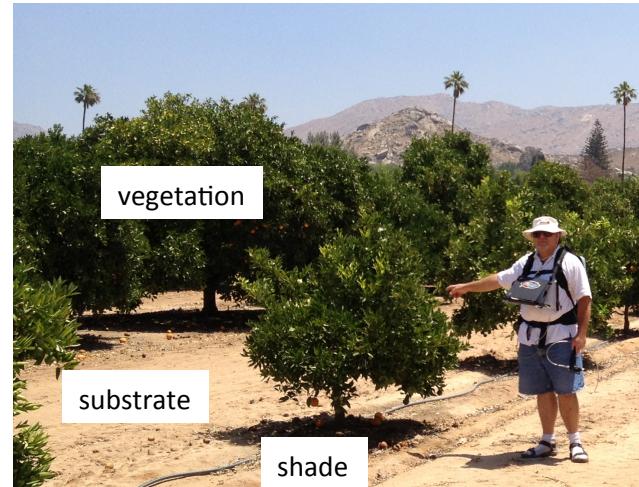
- Diverse species in urban environment (one vs. many classification)
- Complex illumination and substrate



# Our spectral mixture model

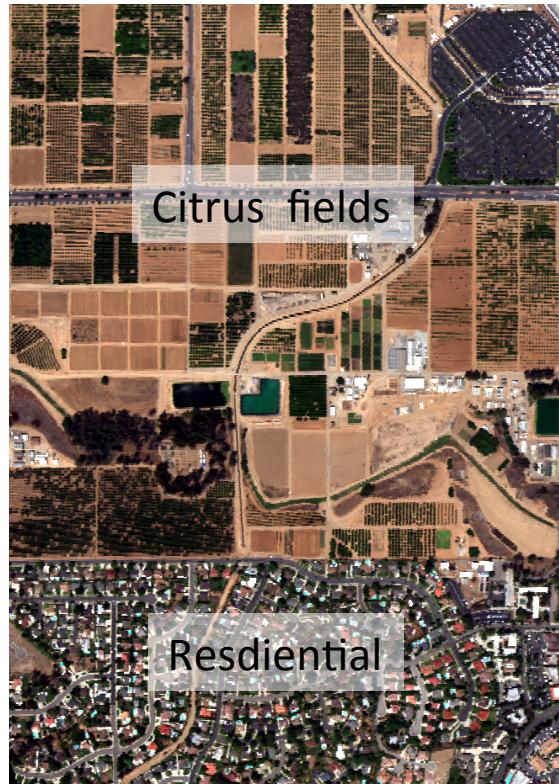
Each spectrum is a combination of three MESMA components:

1. Vegetation
2. Substrate
3. Shade (photometric)

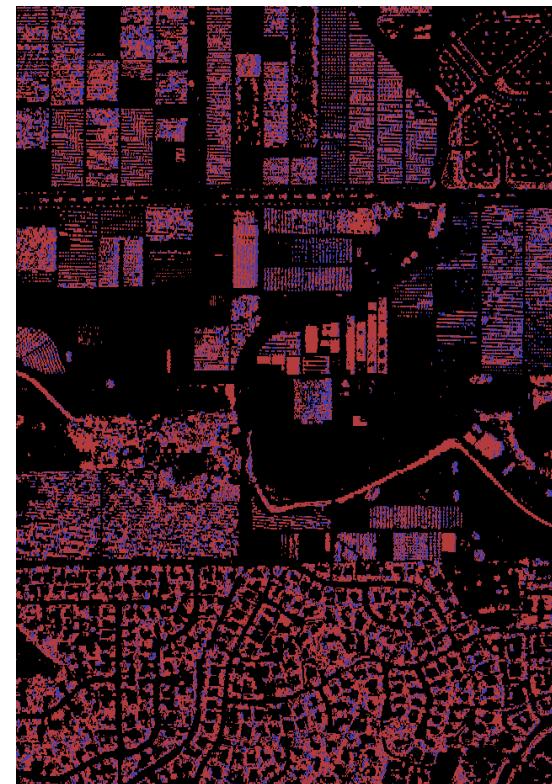


# Initial result for AVIRIS-C data

Original UCR scene



MESMA (library via CoB)



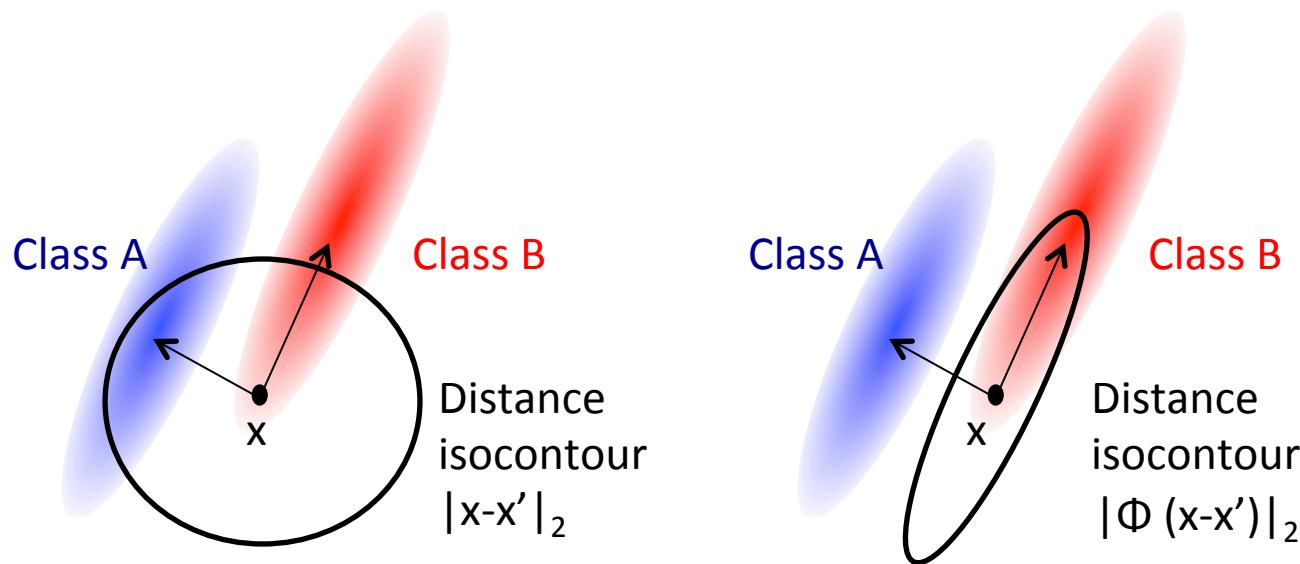
Citrus

Non-citrus



# Non-isotropic distance metrics

- Standard least-squares solutions use an *isotropic* error function (all bands weighted equally)
- However, errors are correlated due to structure in noise and class distributions
- Can we capture this intuition to improve performance?



# Multiclass Discriminants

- Original idea from Fisher [1936],
- Generalized by Rao [1948]
- Calculates a linear projection maximizing class separation

Within-class  
scatter

$$\hat{\Sigma}_w = S_1 + \cdots + S_n = \sum_{i=1}^n \sum_{\mathbf{x} \in c_i} (\mathbf{x} - \bar{\mathbf{x}}_i)(\mathbf{x} - \bar{\mathbf{x}}_i)'$$

Between-class  
scatter

$$\hat{\Sigma}_b = \sum_{i=1}^n m_i (\bar{\mathbf{x}}_i - \bar{\mathbf{x}})(\bar{\mathbf{x}}_i - \bar{\mathbf{x}})'$$



# Multiclass Discriminants

- Original idea from Fisher [1936],
- Generalized by Rao [1948]
- Calculates a linear projection maximizing class separation

Within-class scatter       $\hat{\Sigma}_w = S_1 + \cdots + S_n = \sum_{i=1}^n \sum_{\mathbf{x} \in c_i} (\mathbf{x} - \bar{\mathbf{x}}_i)(\mathbf{x} - \bar{\mathbf{x}}_i)'$

Between-class scatter       $\hat{\Sigma}_b = \sum_{i=1}^n m_i (\bar{\mathbf{x}}_i - \bar{\mathbf{x}})(\bar{\mathbf{x}}_i - \bar{\mathbf{x}})'$

Find  $\Phi$  to maximize       $\mathcal{J}(\Phi) = \frac{|\Phi^T \hat{\Sigma}_b \Phi|}{|\Phi^T \hat{\Sigma}_w \Phi|}$       by solving       $\hat{\Sigma}_b \Phi = \lambda \hat{\Sigma}_w \Phi$



# Procedure

Collect a training set of 30 canopies

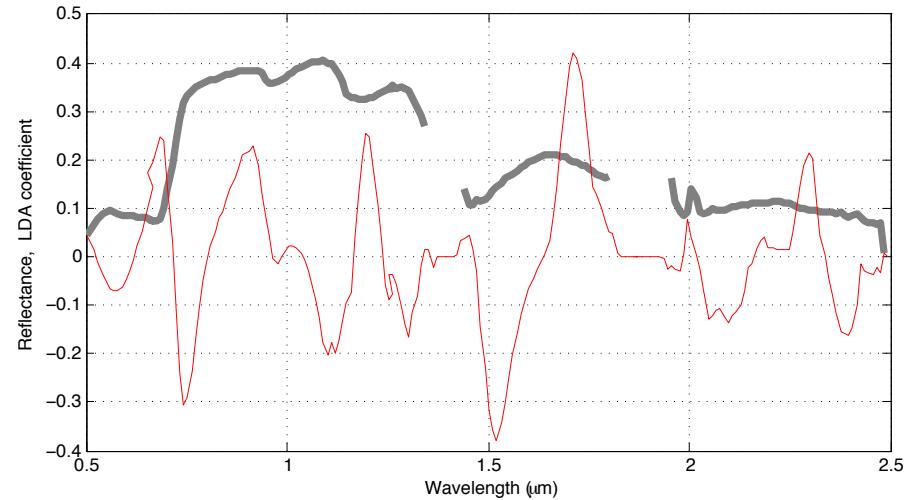
Learn the 10D linear projection to best separate distinct plants

Species-specific projections also possible

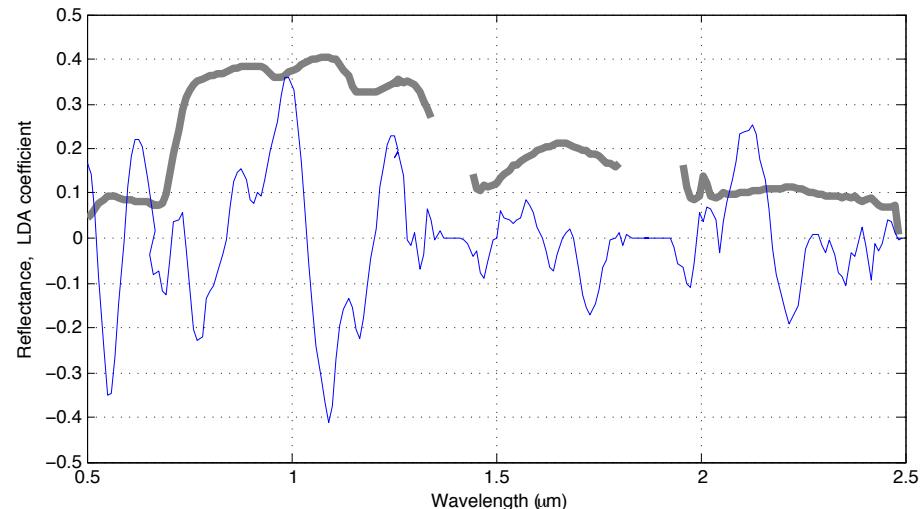
Example labels



Projection for first dimension  $\Phi_1$



Projection for second dimension  $\Phi_1$

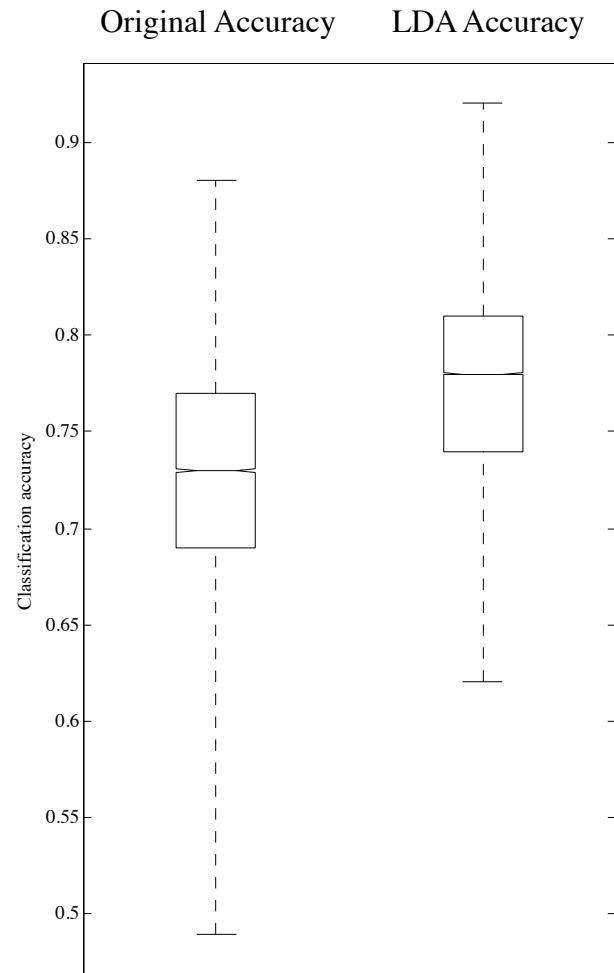
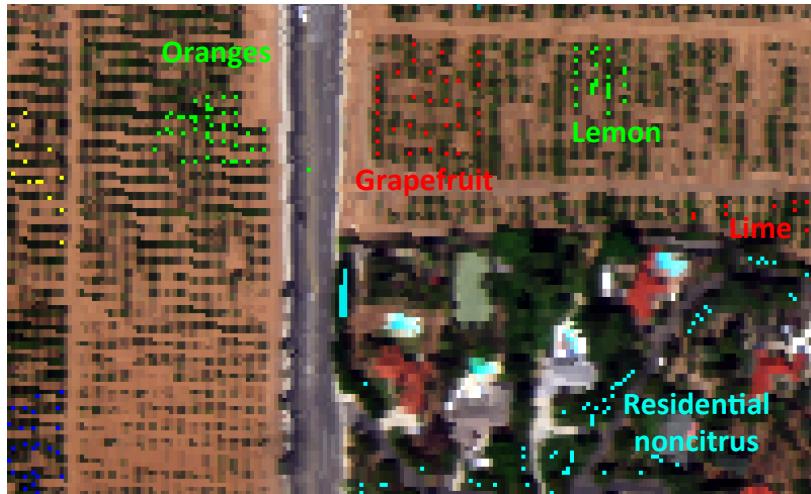


# Simulation

Simulated mixtures of citrus and noncitrus spectra with substrate

Unmixed these spectra using a library randomly decimated by 90%

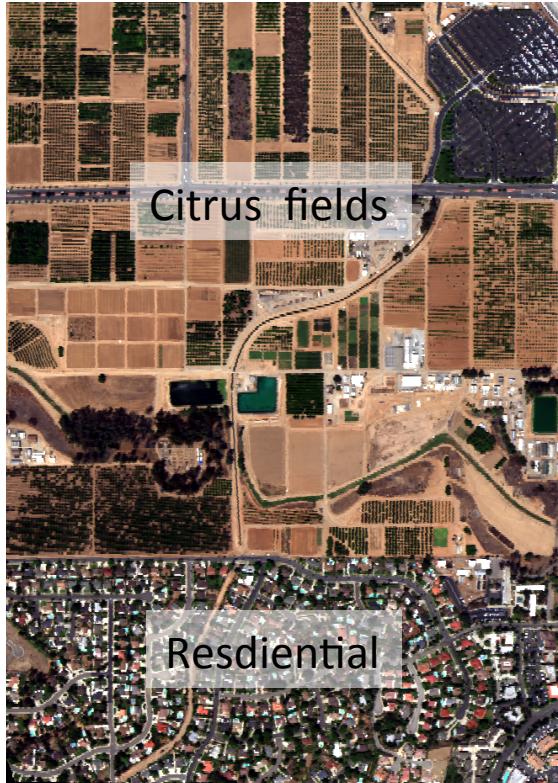
Premultiplication by LDA transform gives a modest but statistically-significant improvement



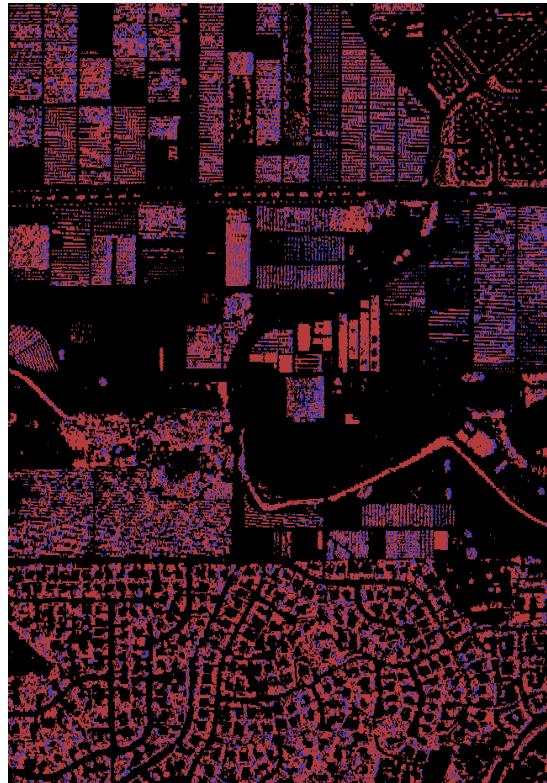
# Impact of MDA (AVIRIS-C)

In practice the improvement is significant

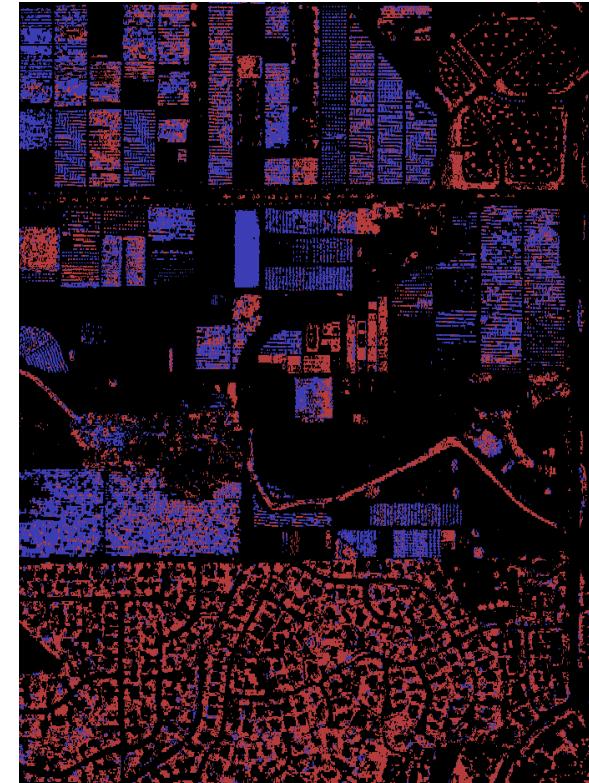
Original scene



MESMA (library via CoB)



With MDA pre-transform



Citrus

Non-citrus

Citrus

Non-citrus



# UCR example using the Next Generation Imaging Spectrometer – an AVIRIS-like instrument

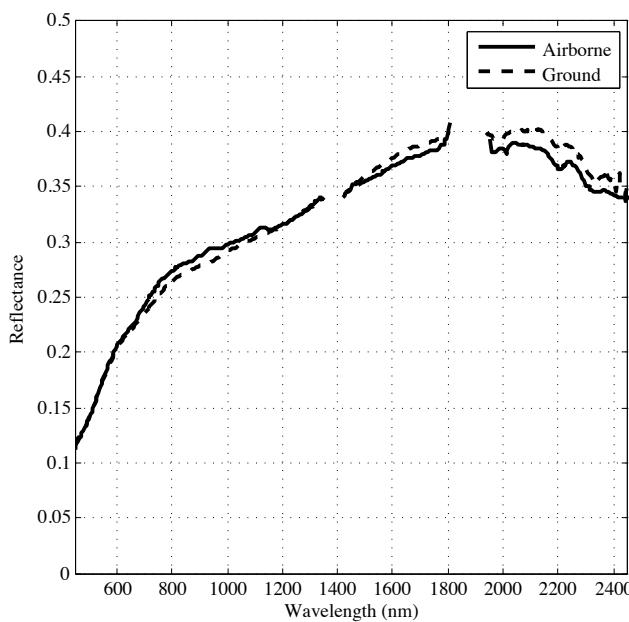


# Reflectance correction using in situ spectra

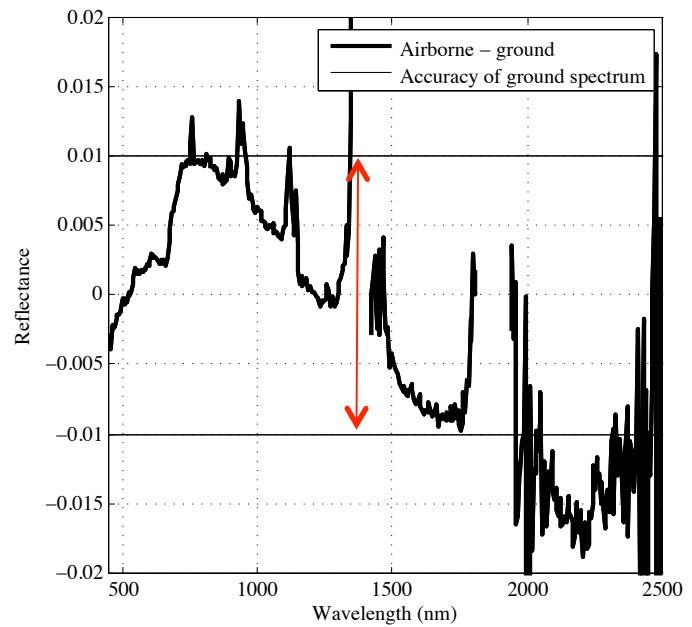
In situ measurement

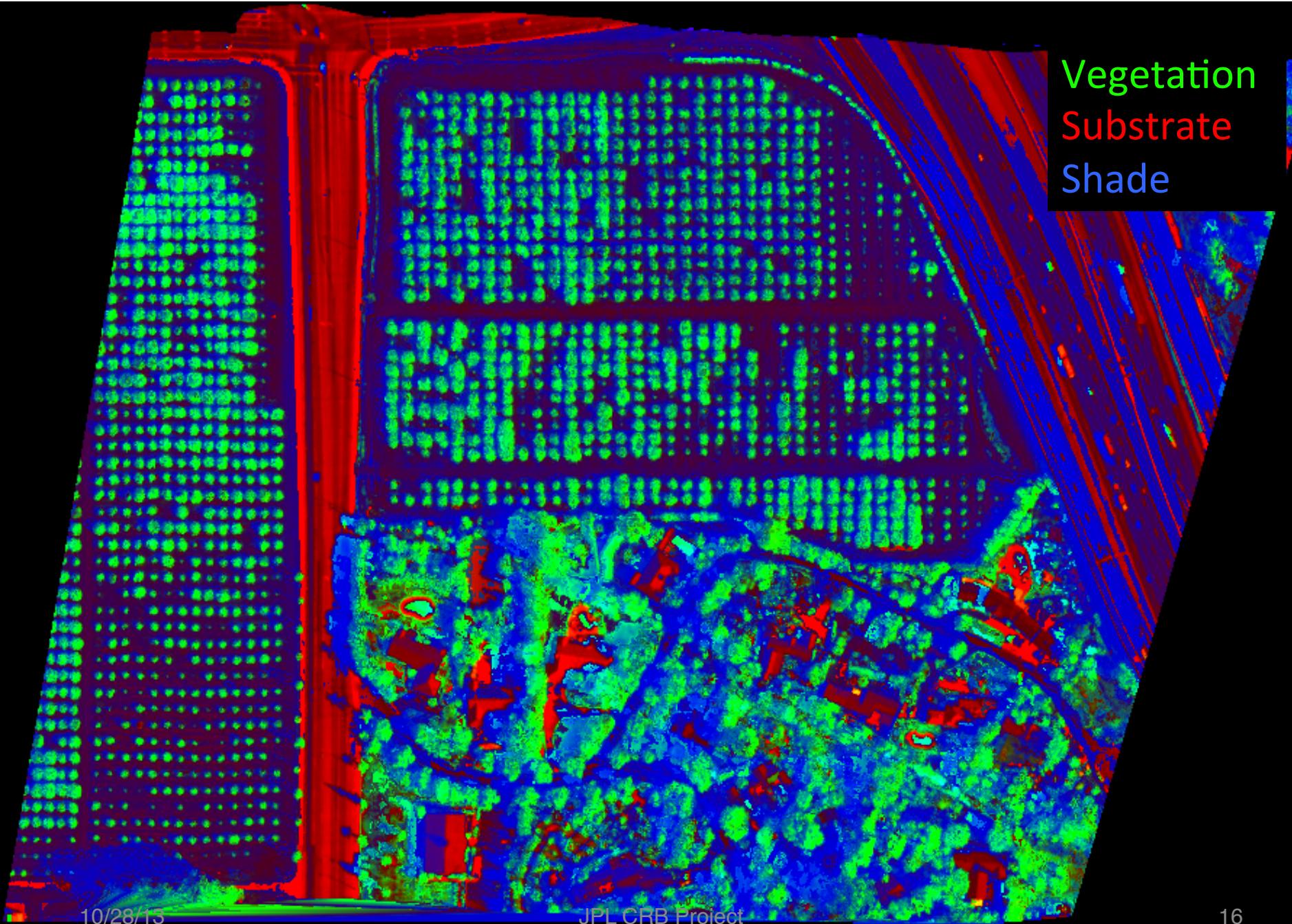


Field 18 road



Agreement, and in situ radiometric accuracy



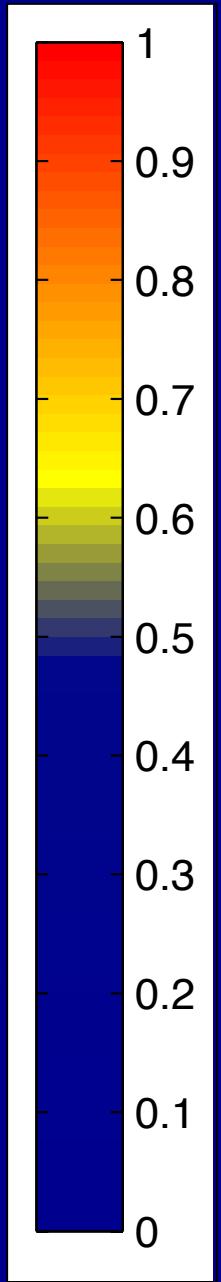
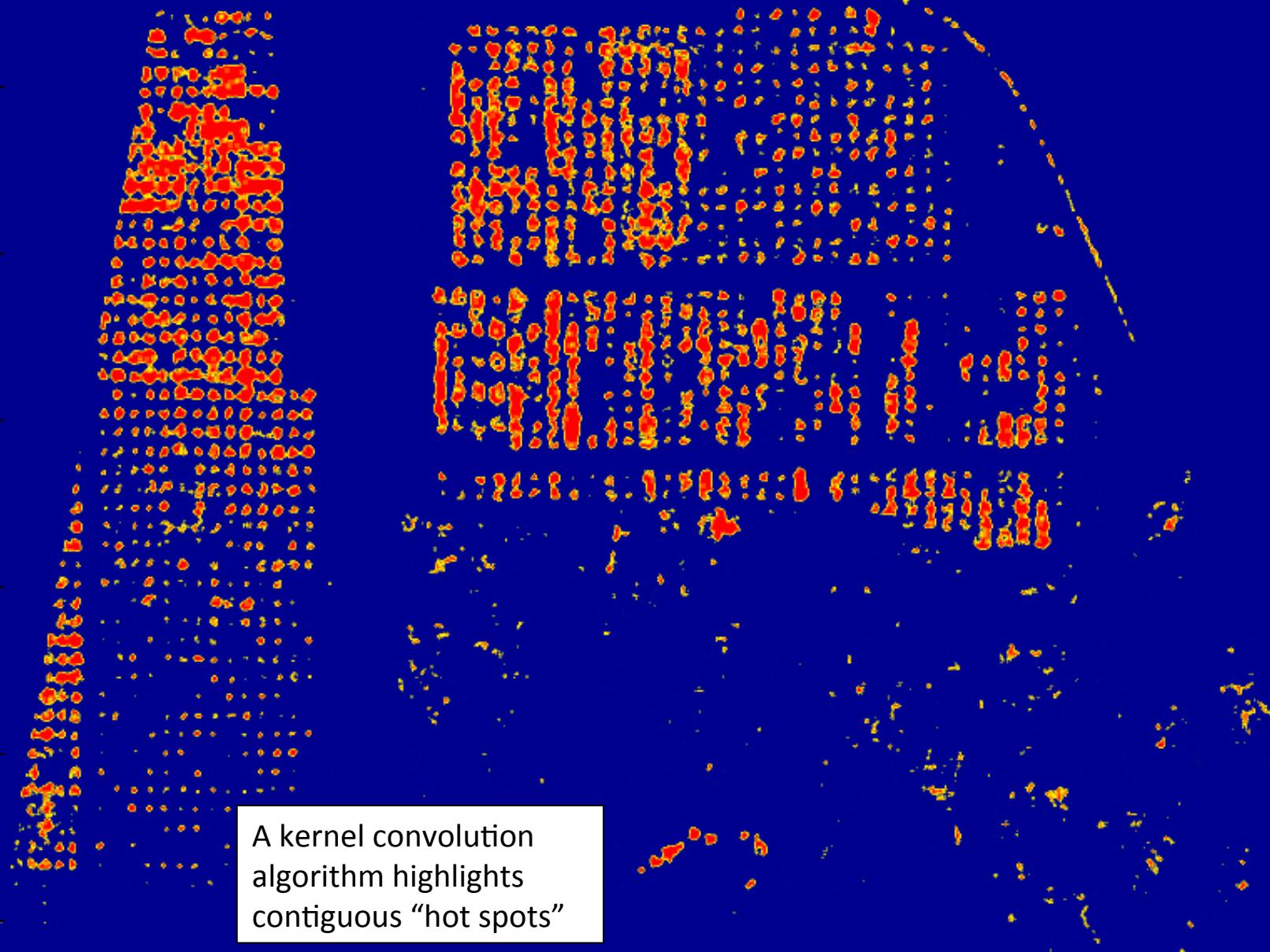


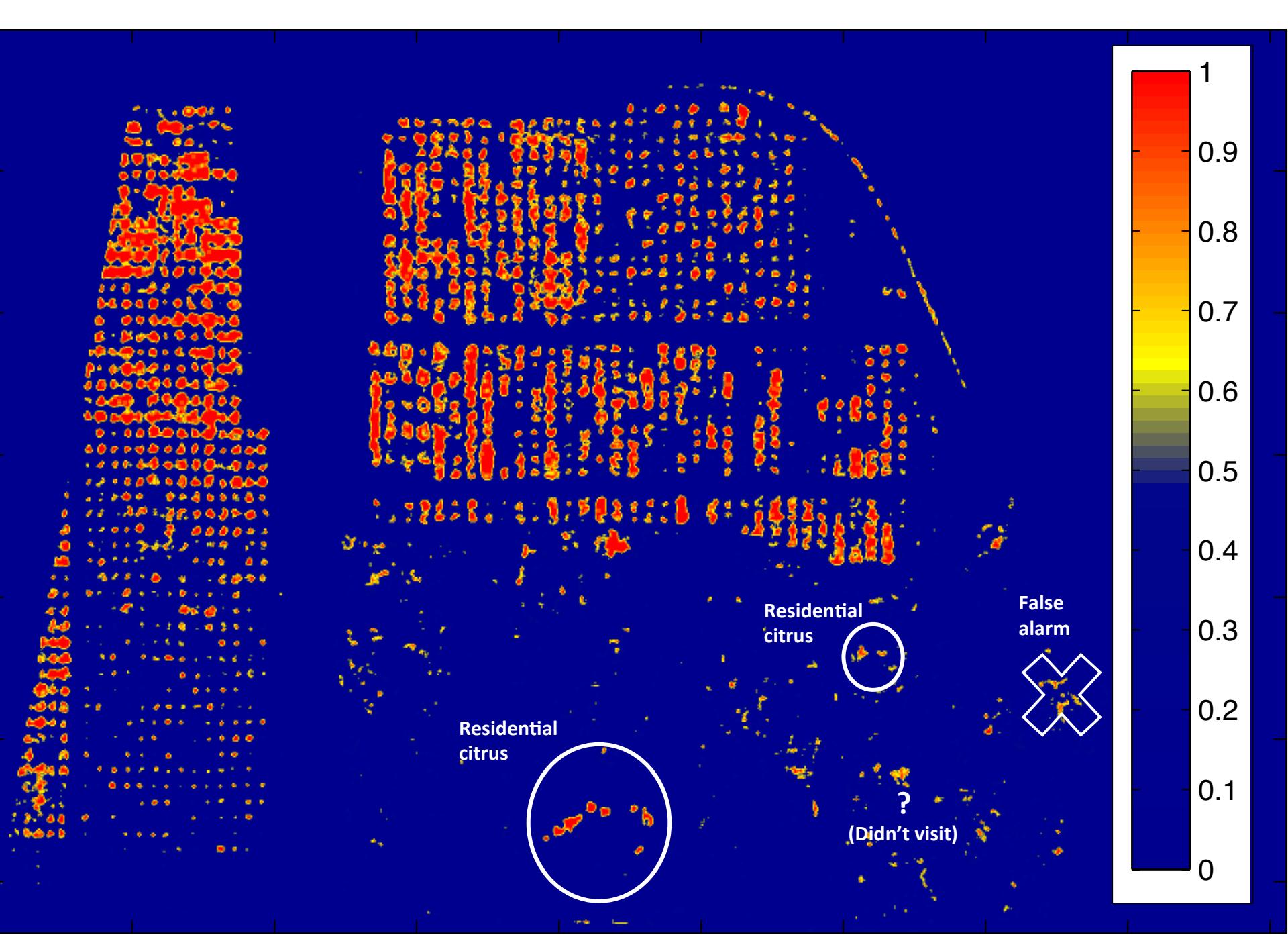
10/28/13

JPL CRB Project

16

We identify citrus plants by fitting each spectrum with the library



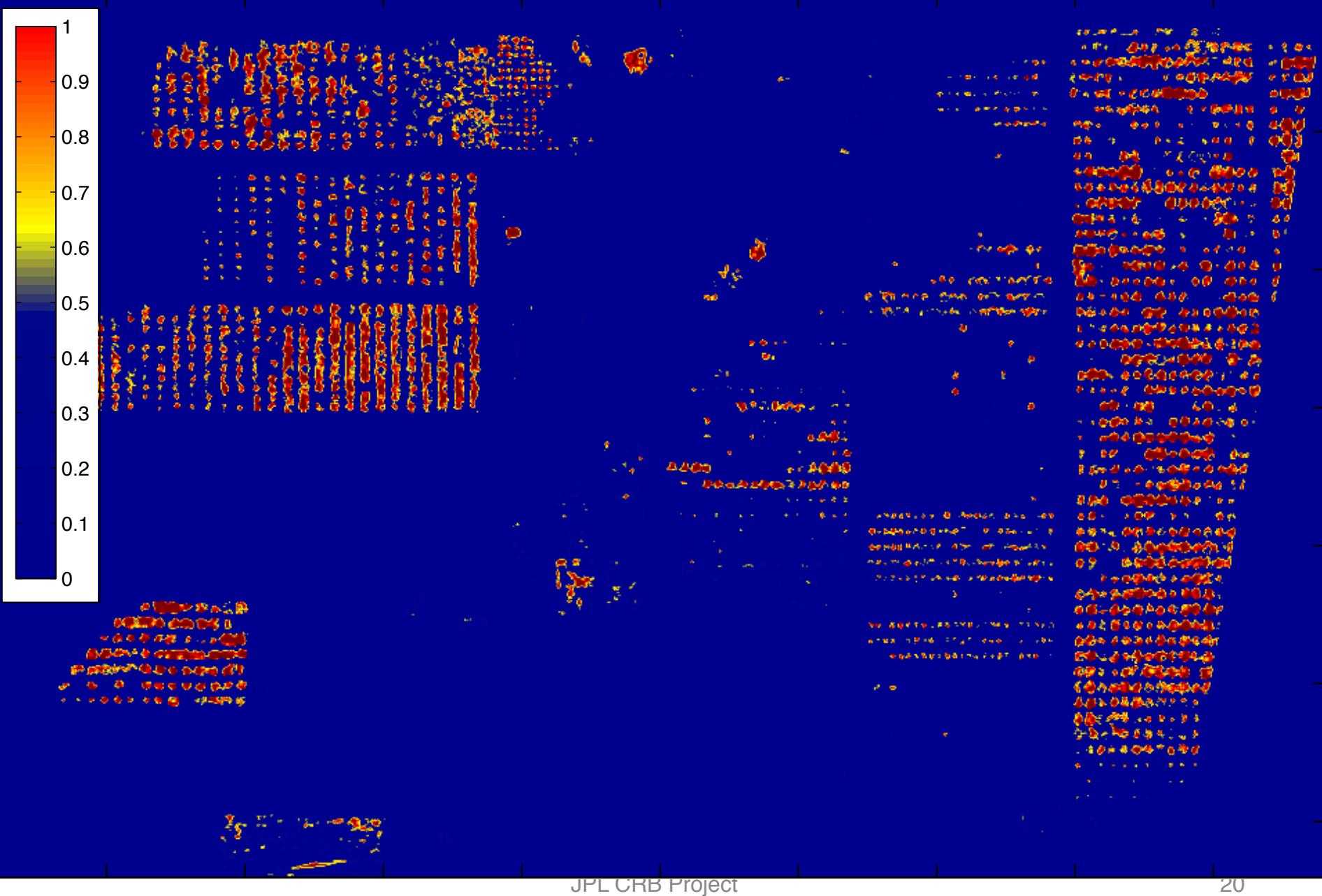




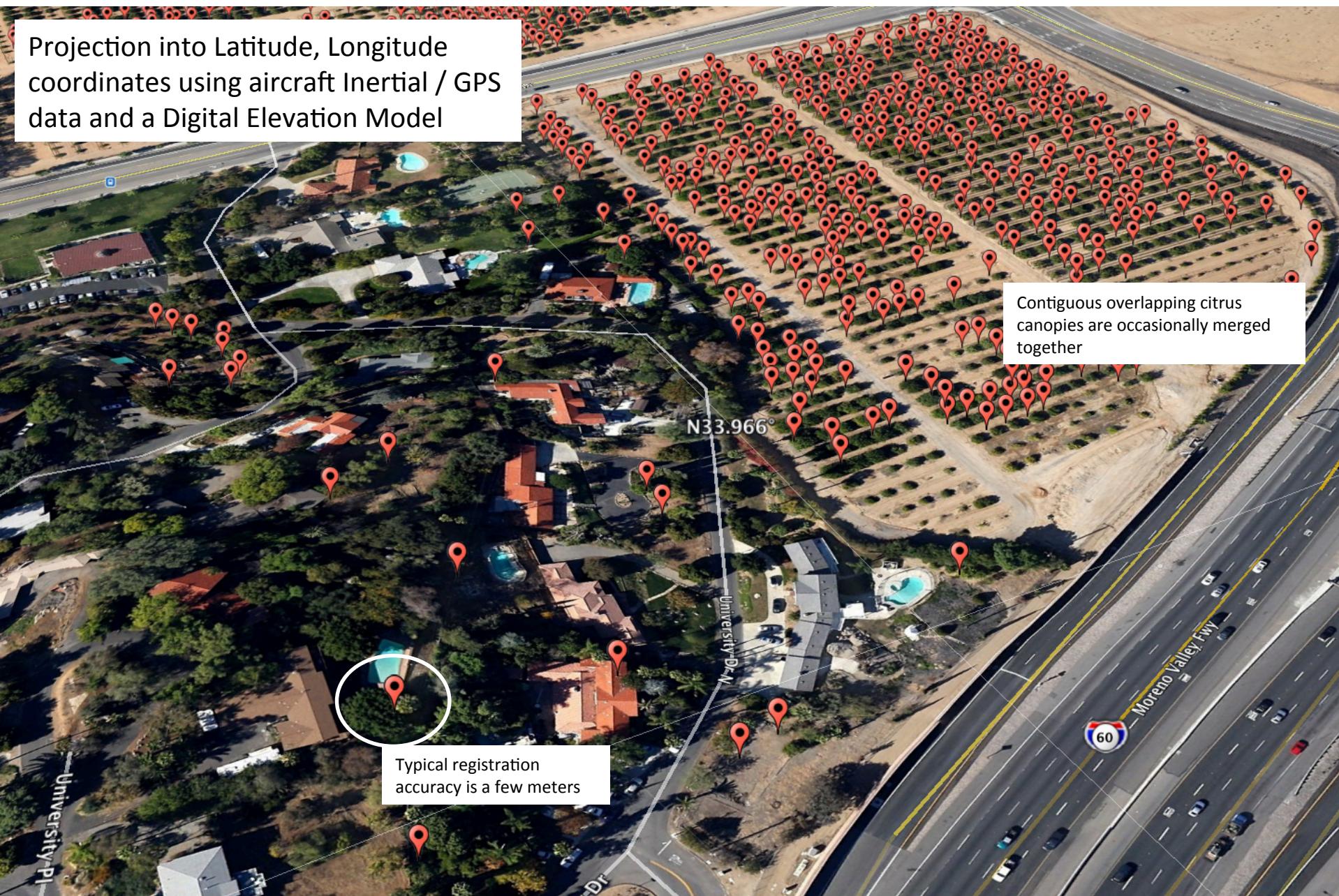
10/28/13

JPL CRB Project

19



Projection into Latitude, Longitude  
coordinates using aircraft Inertial / GPS  
data and a Digital Elevation Model



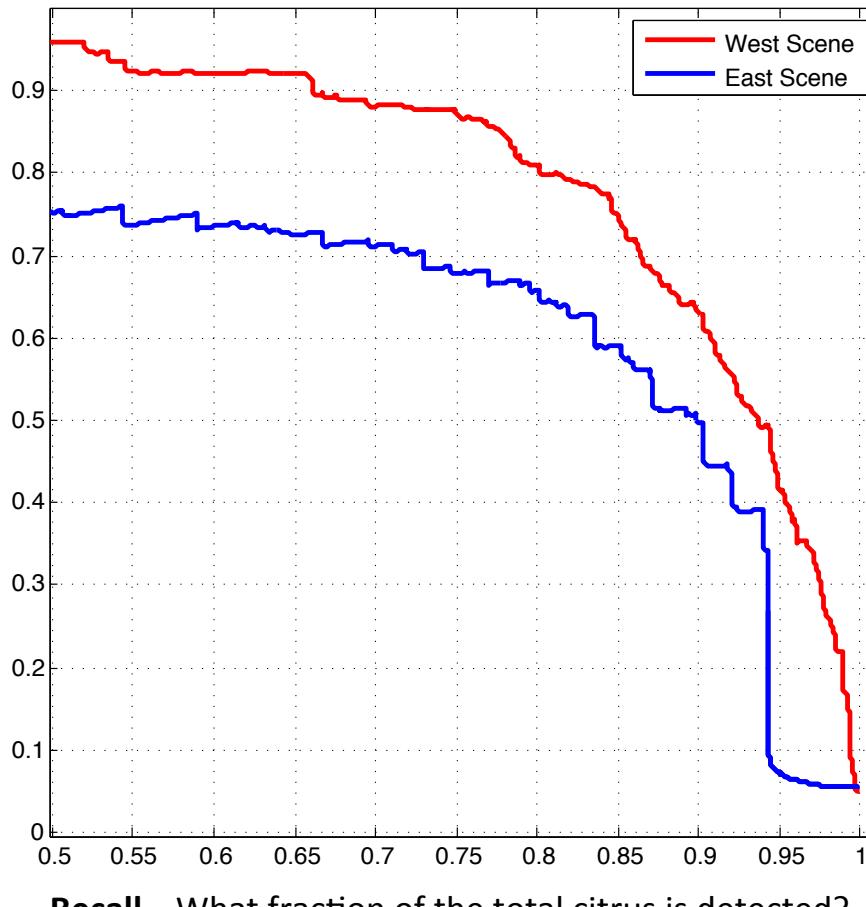
# Performance for citrus plant detection

Detection performance

Assumes 5% of trees are citrus

Precision

What fraction of detections are real?



Recall What fraction of the total citrus is detected?

Confusion matrices

East Scene

		Actual	
		Non-citrus	Citrus
Predicted	Non-citrus	350	156
	Citrus	31	966

West Scene

		Actual	
		Non-citrus	Citrus
Predicted	Non-citrus	395	243
	Citrus	23	1260



Jet Propulsion Laboratory  
California Institute of Technology

# Questions?



Jet Propulsion Laboratory  
California Institute of Technology

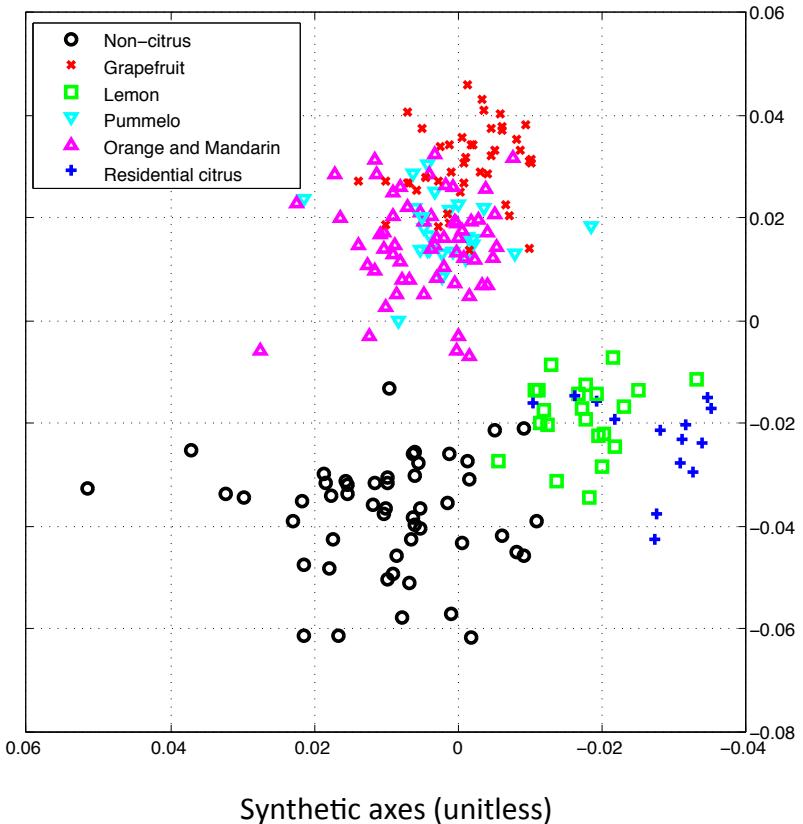
# Backup slides

# Examples of residential citrus from UCR neighborhood survey

We use Linear Discriminant Analysis to represent the spectral data in a way that emphasizes cross-plant differences

Discriminant Analysis suggests the spectra are:

- Somewhat similar to cultivated citrus plants
- Distinct from non-citrus residential plants



# Spectral derivatives

Suggest several candidate diagnostic features

